



**ADVANCED SUBSIDIARY GCE UNIT  
MATHEMATICS (MEI)**

Concepts for Advanced Mathematics (C2)

**THURSDAY 7 JUNE 2007**

**4752/01**

Morning  
Time: 1 hour 30 minutes

Additional materials:

Answer booklet (8 pages)

Graph paper

MEI Examination Formulae and Tables (MF2)

**INSTRUCTIONS TO CANDIDATES**

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

**INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks for this paper is 72.

**ADVICE TO CANDIDATES**

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.

This document consists of **6** printed pages and **2** blank pages.

## 2

## Section A (36 marks)

1 (i) State the exact value of  $\tan 300^\circ$ . [1]

(ii) Express  $300^\circ$  in radians, giving your answer in the form  $k\pi$ , where  $k$  is a fraction in its lowest terms. [2]

2 Given that  $y = 6x^{\frac{3}{2}}$ , find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$ .

Show, without using a calculator, that when  $x = 36$  the value of  $\frac{d^2y}{dx^2}$  is  $\frac{3}{4}$ . [5]

3

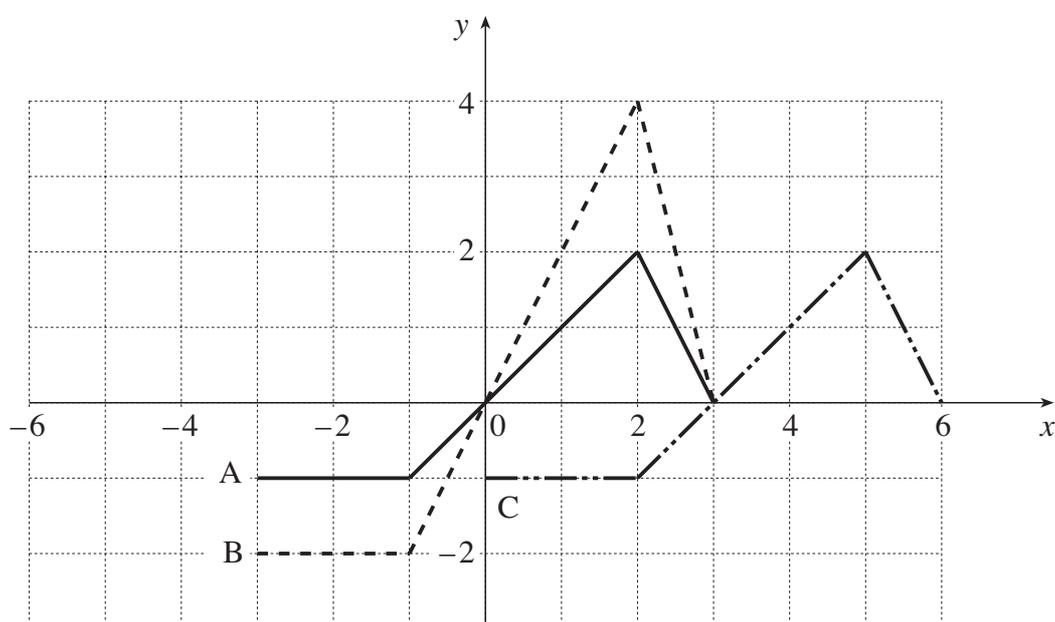


Fig. 3

Fig. 3 shows sketches of three graphs, A, B and C. The equation of graph A is  $y = f(x)$ .

State the equation of

(i) graph B, [2]

(ii) graph C. [2]

## 3

- 4 (i) Find the second and third terms of the sequence defined by the following.

$$\begin{aligned}t_{n+1} &= 2t_n + 5 \\ t_1 &= 3\end{aligned}\quad [2]$$

- (ii) Find  $\sum_{k=1}^3 k(k+1)$ . [2]

- 5 A sector of a circle of radius 5 cm has area  $9 \text{ cm}^2$ .

Find, in radians, the angle of the sector.

Find also the perimeter of the sector. [5]

- 6 (i) Write down the values of  $\log_a 1$  and  $\log_a a$ , where  $a > 1$ . [2]

- (ii) Show that  $\log_a x^{10} - 2\log_a \left(\frac{x^3}{4}\right) = 4\log_a(2x)$ . [3]

- 7 (i) Sketch the graph of  $y = 3^x$ . [2]

- (ii) Use logarithms to solve the equation  $3^x = 20$ . Give your answer correct to 2 decimal places. [3]

- 8 (i) Show that the equation  $2 \cos^2 \theta + 7 \sin \theta = 5$  may be written in the form

$$2 \sin^2 \theta - 7 \sin \theta + 3 = 0. \quad [1]$$

- (ii) By factorising this quadratic equation, solve the equation for values of  $\theta$  between  $0^\circ$  and  $180^\circ$ . [4]

### Section B (36 marks)

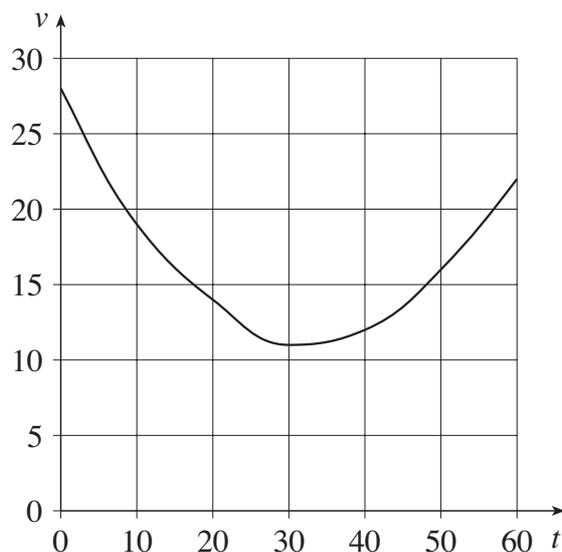
- 9 The equation of a cubic curve is  $y = 2x^3 - 9x^2 + 12x - 2$ .

- (i) Find  $\frac{dy}{dx}$  and show that the tangent to the curve when  $x = 3$  passes through the point  $(-1, -41)$ . [5]

- (ii) Use calculus to find the coordinates of the turning points of the curve. You need not distinguish between the maximum and minimum. [4]

- (iii) Sketch the curve, given that the only real root of  $2x^3 - 9x^2 + 12x - 2 = 0$  is  $x = 0.2$  correct to 1 decimal place. [3]

- 10** Fig. 10 shows the speed of a car, in metres per second, during one minute, measured at 10-second intervals.



**Fig. 10**

The measured speeds are shown below.

Time ( $t$ seconds)	0	10	20	30	40	50	60
Speed ( $v$ $\text{ms}^{-1}$ )	28	19	14	11	12	16	22

- (i) Use the trapezium rule with 6 strips to find an estimate of the area of the region bounded by the curve, the line  $t = 60$  and the axes. [This area represents the distance travelled by the car.] [4]
- (ii) Explain why your calculation in part (i) gives an overestimate for this area. Use appropriate rectangles to calculate an underestimate for this area. [3]

The speed of the car may be modelled by  $v = 28 - t + 0.015t^2$ .

- (iii) Show that the difference between the value given by the model when  $t = 10$  and the measured value is less than 3% of the measured value. [2]
- (iv) According to this model, the distance travelled by the car is

$$\int_0^{60} (28 - t + 0.015t^2) dt.$$

Find this distance.

[3]

## 5

**11 (a)** André is playing a game where he makes piles of counters. He puts 3 counters in the first pile. Each successive pile he makes has 2 more counters in it than the previous one.

**(i)** How many counters are there in his sixth pile? [1]

**(ii)** André makes ten piles of counters. How many counters has he used altogether? [2]

**(b)** In another game, played with an ordinary fair die and counters, Betty needs to throw a six to start.

The probability  $P_n$  of Betty starting on her  $n$ th throw is given by

$$P_n = \frac{1}{6} \times \left(\frac{5}{6}\right)^{n-1}.$$

**(i)** Calculate  $P_4$ . Give your answer as a fraction. [2]

**(ii)** The values  $P_1, P_2, P_3, \dots$  form an infinite geometric progression. State the first term and the common ratio of this progression.

Hence show that  $P_1 + P_2 + P_3 + \dots = 1$ . [3]

**(iii)** Given that  $P_n < 0.001$ , show that  $n$  satisfies the inequality

$$n > \frac{\log_{10} 0.006}{\log_{10} \left(\frac{5}{6}\right)} + 1.$$

Hence find the least value of  $n$  for which  $P_n < 0.001$ . [4]